REYNOLDS NUMBER DEPENDENCE OF LARGE-SCALE FRICTION CONTROL
IN TURBULENT CHANNEL FLOW

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INTRODUCTION
The search for an effective mean of reducing turbulent skin-friction drag is one of the most active fields of research in fluid mechanics. The benefits of efficient flow control are numerous: from energy and economical savings, to more efficient and greener machinery, be it aviation or fluid transport and mixing [5]. Several techniques have been investigated, ranging from passive methods such as riblets [6], to active control strategies as, for example, streamwise-travelling waves of spanwise wall velocity [15], uniform blowing and suction [10], volume forcing [13], and direct modification of the mean flow [16]. Most of these control techniques, though, have been analysed only at low Reynolds numbers ($Re_\tau$) and only recently some authors have started investigating the effects that an increasing Reynolds number has on the flow control strategy (see, for instance, Refs. [9, 8, 7]).

One of the more promising techniques consists of the large-scale vortices proposed by Schoppa & Hussain [16] which (in the original study) were embedded in a turbulent channel flow at a friction Reynolds number $Re_\tau$ = 104, where turbulence is marginally sustainable. This drag reduction strategy was found to be ineffective by Canton et al. [1], since the claimed drag-reduction effect was shown to be of transient nature. Nonetheless, Canton et al. [1] recast the method as a volume forcing control for channel flows that lead to sustainable drag reduction at $Re_\tau$ = 180. These large-scale vortices were promoted by their original authors as a promising, feed-forward or passive, control technique capable of reducing the turbulent friction drag from the outside of the viscous layer, and thus, independent of the small scales of wall turbulence, which would otherwise limit its applicability to practically relevant Reynolds numbers due to sensor/actuator limitations [11].

It is well known, though, that near-wall structures scale with viscous units (see e.g. Ref. [12]) and that low Reynolds number effects are present in wall-bounded flows at least up to $Re_\tau$ = 395 [14]. Moreover, it has been found that the performance of different control strategies deteriorates as the Reynolds number is increased; this is the case at least for the active V- and suboptimal control schemes [9] and the oscillating wall and travelling waves [8, 7]. These two observations provide the main motivation for the present analysis.

NUMERICAL SETUP
This work is concerned with direct numerical simulations (DNS) of incompressible channel flows at fixed bulk Reynolds number $Re_b$, based on bulk velocity $U_b$, channel half-height $h$ and fluid viscosity $\nu$. Four values of bulk Reynolds number are employed: $Re_b = 1518, 2800, 6240$ and $10000$, such as to

$$Re_\tau \quad \text{Integration time} \quad \text{Domain size} \quad \text{Grid points}$$

<table>
<thead>
<tr>
<th>$Re_\tau$</th>
<th>Integration time</th>
<th>Domain size</th>
<th>Grid points</th>
</tr>
</thead>
<tbody>
<tr>
<td>104</td>
<td>10500</td>
<td>8, 3.832</td>
<td>48, 65, 48</td>
</tr>
<tr>
<td>180</td>
<td>1500</td>
<td>12, 6.6</td>
<td>128, 97, 96</td>
</tr>
<tr>
<td>360</td>
<td>1000</td>
<td>12, 6.6</td>
<td>300, 151, 200</td>
</tr>
<tr>
<td>550</td>
<td>400</td>
<td>12, 6.6</td>
<td>432, 193, 300</td>
</tr>
</tbody>
</table>

Table 1: Details of the numerical discretisation employed for the present simulations. $T$ corresponds to the duration of the controlled simulations; $N_x$ and $N_z$ represent the number of Fourier modes employed in the wall-parallel directions (values before dealiasing), while $N_y$ is the order of the Chebyshev expansion used for the wall-normal direction.

result in a friction Reynolds number, based on friction velocity $u_\tau$, $h$ and $\nu$, corresponding to $Re_\tau \approx 104, 180, 360$ and $550$, where the lowest Reynolds number corresponds to the value employed in the original study by Schoppa & Hussain [16]. The simulations are performed using the pseudo spectral code \textsc{simson} [3]. Details of the domain sizes and spatial resolutions used for the four sets of simulations are reported in table 1.

The large-scale vortices, provided with variable intensity and spanwise wavelength, are imposed via a volume forcing defined as:

$$f_x = 0,$$

$$f_y(y, z) = A\beta \cos(\beta z)(1 + \cos(\pi y/h)), \quad (1)$$

$$f_z(y, z) = A\pi/h \sin(\beta z) \sin(\pi y/h),$$

where $A$ is the forcing amplitude and $\beta$ the wavenumber along $z$. The wavenumber was chosen such as to have vortex periods $\Lambda = 2\pi/\beta$ between $1.1h$ and $9.9h$, corresponding to inner-scaled wavelengths $\Lambda^+$ between 120 and 3630. Here and in

Figure 1: Instantaneous flow field of a controlled simulation for $Re_\tau = 550$ illustrating the large-scale vortices. The figure depicts two vortex wavelengths, with $\Lambda = 3.3h$, on a cross-stream channel plane coloured by streamwise velocity magnitude. The control amplitude is max $|\langle v \rangle_{x,z}| \approx 0.07U_b$.  


the following, all inner-scaled quantities are referred to the uncontrolled case and are indicated with a plus sign, i.e. (·)+.

A sketch of the control vortices for $\Lambda = 3.3 \text{h}$ is depicted in Figure 1. Since $A$ does not correspond to a measurable flow quantity, the maximum wall-normal mean velocity is used to characterise the strength of the vortices, i.e. $\max \langle |v|_{x,t} \rangle/U_\infty$, where $\langle \cdot \rangle_{x,t}$ denotes the average in the streamwise direction and time.

**ANALYSIS AND RESULTS**

A total of 222 controlled simulations have been performed varying the Reynolds number, the control amplitude and the wavelength of the vortices. As shown in Ref. [1], the control scheme is effective at both $Re_*=104$ and 180. For these values of the Reynolds number a drag reduction of up to 16% and 18%, respectively, can be achieved. The performance of the large-scale vortices, though, degrades rapidly: for $Re_*=360$ the maximum DR is only 8%, and for $Re_*=550$ no more than 0.4% ± 0.28% can be obtained [2]. The present analysis covers the entire range of control amplitudes and reasonable vortex wavelengths, the drag reduction values presented are, therefore, the highest achievable under optimal conditions. This result is in agreement with Ref. [4], which shows that selectively damping small-scale fluctuations in a turbulent channel flow for $Re_*=640$ is more effective than damping their large-scale counterparts, albeit their control strategy is different from the present approach based on Ref. [16].

The drag reduction including its uncertainty is illustrated in Figure 2 where panel (a) (in semi-log scale) shows the maximum achievable value of DR as a function of the Reynolds number. Panels (b–e) show the details at each Reynolds number by presenting the performance of the control strategy for $Re_*=104, 180$ and 360 as a function of forcing amplitude and vortex wavelength. Since the method under investigation is an active control scheme, the power used to generate and sustain the large-scale vortices needs to be taken into account for a complete assessment of the performance. The net power saving rate is defined as $S = (P_{\text{unc}} - P_{\text{con}})/P_{\text{unc}} = DR - P_{\text{con}}/P_{\text{unc}}$, where $P_{\text{unc}}$ is the power required to drive the uncontrolled channel flow, while $P_{\text{con}}$ is the power needed by the control, computed for an ideal actuator as $P_{\text{con}} = 1/(\Omega T) \int_0^{T} \rho U_\infty F \cdot \dot{v} \, dt \, dt_1$. As it can be observed in Figure 2(a), the Reynolds-number dependence of this figure of merit is qualitatively similar to that of DR, confirming that the large-scale vortices perform well for low Reynolds numbers but fail to provide a positive effect for $Re_*>550$. In particular, it was observed that the energy consumed by the ideal actuators does not significantly affect the parameters for the control: both the optimal wavelength and the forcing amplitude exhibit the same values compared to when not considering the power used to generate the large-scale vortices.

The final contribution will include a complete study on the causes that lead the method to become ineffective for high $Re$. Different aspects of the interaction between the control mechanism and the underlying flow will be analysed in order to shed light on the DR($Re$) trend.

**REFERENCES**


