

FIG. 1. Views from above (left) and side (right) of the limit cycle for R = 1, R = 2 and R = 3 (top to bottom), showing volume rendering of the  $\lambda_2$  vortex identification criterion<sup>1</sup>.



FIG. 2. The unstable global eigenmode and its corresponding adjoint mode (a) and the 'wavemaker' (b) at R = 0.7.

## Stability of a jet in crossflow

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We study direct numerical simulations (DNS) of a jet in crossflow at low values of the jet-to-crossflow velocity ratio R. As R is increased, the flow evolves from simple periodic vortex shedding (a limit cycle) to more complicated quasiperiodic behavior, before finally becoming turbulent (Fig. 1), as seen in previous simulations<sup>2,3</sup>, and in the included video. The first bifurcation is found to occur at  $R \approx 0.7$ , and the observed shedding of hairpin vortices is possibly linked to a possible existence of a local absolute instability of the shear layer immediately downstream of the jet. We focus on this first bifurcation, and find that a global linear stability analysis pre-

dicts exactly the frequency and initial growth rate of the nonlinear DNS simulation at R = 0.7. In addition, we compute the adjoint global eigenmodes, and find that the overlap of the most unstable and the corresponding adjoint eigenmode, also known as a 'wavemaker' (Fig. 2), provides additional evidence that the source of the first instability indeed lies in the shear layer above the reversed flow region downstream of the orifice.

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<sup>&</sup>lt;sup>1</sup>J. Jeong and F. Hussain. On the identification of a vortex. *Journal of Fluid Mechanics*, 285:69–94, 1995.